

A diffraction grating has $2000 \frac{\text{lines}}{\text{cm}}$.

What is the angle between the 1st-order maxima for red light ($\lambda = 680\text{nm}$) and blue light ($\lambda = 410\text{nm}$)?

$$N = 2000 \frac{\text{lines}}{\text{cm}}$$

$$n = 1$$

$$d \sin \theta = n \lambda$$

$$\sin \theta = \frac{n \lambda}{d} = n \lambda N$$

blue

$$\theta = \sin^{-1}(n \lambda N)$$

$$= \sin^{-1}(1 (410 \times 10^{-9}) 2.0 \times 10^5)$$

$$= 4.7^\circ$$

red

$$\theta = \sin^{-1}(n \lambda N)$$

$$= \sin^{-1}(1 (680 \times 10^{-9}) 2 \times 10^5)$$

$$= ~~8.6~~ 7.8^\circ$$

$$7.8^\circ - 4.7^\circ = \boxed{3.1^\circ}$$

Determine the longest wavelength that can produce a third order maximum using a diffraction grating with $630 \frac{\text{lines}}{\text{mm}}$.

$$N = 630 \frac{\text{lines}}{\text{mm}}$$

$$d \sin \theta = n \lambda$$

$$n = 3$$

$$\cancel{\sin \theta}$$

$$\frac{d \cancel{\sin \theta}}{n} = \lambda$$

$$\frac{\cancel{\sin \theta}}{N n} = \lambda$$

$$\frac{1}{\left(630 \frac{\text{lines}}{\text{mm}}\right) 3} = \lambda = 5.29 \text{ E-}4 \text{ mm}$$

$$\boxed{529 \text{ nm}}$$

White light strikes a diffraction grating with $6700 \frac{\text{lines}}{\text{cm}}$ at normal incidence.

How many complete spectra will be formed on either side of the central maximum?

violet $\lambda = 400\text{nm}$

Red $\lambda = 700\text{nm}$

$$N = 6700 \frac{\text{lines}}{\text{cm}}$$

$$d \sin \theta = n \lambda$$

$$d = n \lambda$$

$$n = \frac{d}{\lambda} = \frac{1}{N \lambda}$$

Note:

Since

$$\theta = \sin^{-1} \left(\frac{n \lambda}{d} \right)$$

red will be diffracted the most.

$$n = \frac{1}{\left(6700 \frac{\text{lines}}{\text{cm}} \right) \left(700 \times 10^{-7} \text{cm} \right)}$$

$$= 2.13$$

2 complete spectra