

Torque

①

For translation a force is required to change an object's state of motion.

The same is true for rotation, but the force must ~~to~~ have a particular orientation.



Torque is the rotational equivalent of force

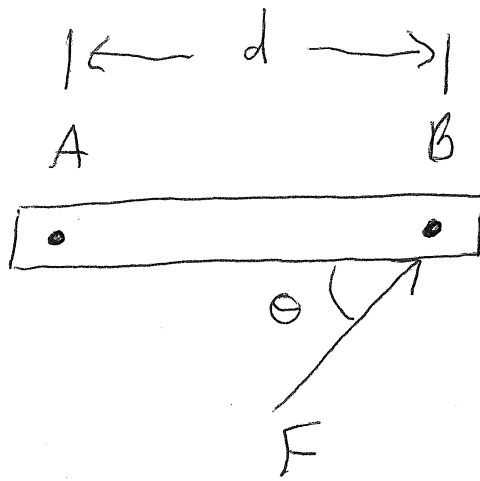
$$\tau = Fd$$

F = applied force \perp to d (N)

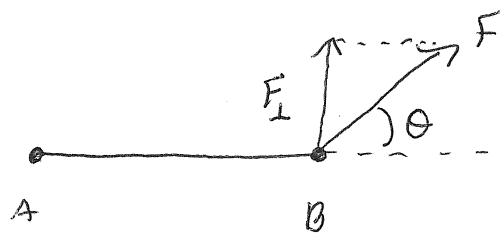
d = distance F is applied from a point of rotation (m)

Unit for torque

Nm



The torque is calculated using the component of force that is perpendicular to the lever-arm.

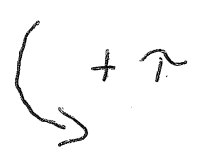
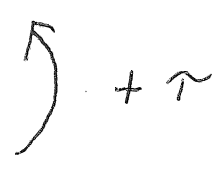


$$F_{\perp} = F \sin \theta$$

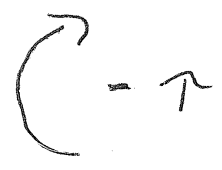
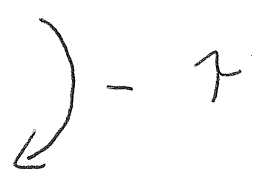
Notice that some point must be defined as the point of rotation.

(A in this case)

Torque Sign convention



counter-clockwise



clockwise

Recall:

Translation

Rotation

x

θ

v

ω

a

α

m

I

F

τ



$$F = ma$$

$$\tau = I\alpha$$

m = mass (kg)

I = rotational inertia (kgm^2)

a = acceleration ($\frac{\text{m}}{\text{s}^2}$)

α = angular acceleration ($\frac{\text{rad}}{\text{s}^2}$)

F = force (N)

τ = torque (Nm)

Static Equilibrium

Recall that previously we defined static Equilibrium as $\Sigma F = 0$.

Now we must also account for rotation.

Static Equilibrium

$$\Sigma F = 0 \quad \text{and} \quad \Sigma \tau = 0$$



sum of all forces



sum of all torques