

# Heat Engine

- Device that is used to extract energy from the environment to do useful work.

\* The working substance in an engine must operate in a cycle.

↘ closed series of thermodynamic processes

In an ideal engine:

- All processes are reversible
- no wasteful energy transfers.

# Thermodynamic Processes

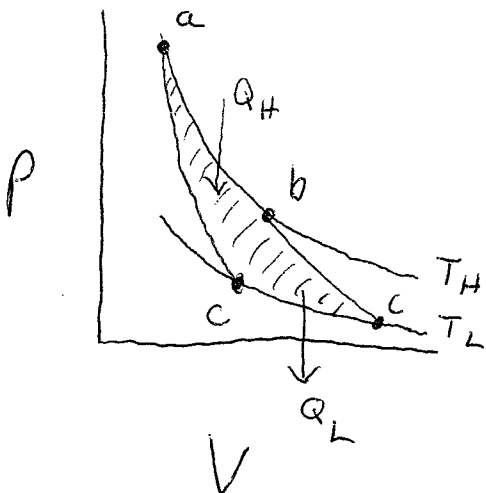
- 1) isothermal Expansion  $\Delta E_{int} = 0$   $\downarrow P \uparrow V - T$   $Q = W$
- 2) adiabatic Expansion  $Q = 0$   $\downarrow P \downarrow T \uparrow V$   $\Delta E_{int} = -W$   
( $\downarrow E_{int} \uparrow W$ )
- 3) isothermal Compression  $\Delta E_{int} = 0$   $\uparrow P \downarrow V - T$   $Q = W$
- 4) adiabatic Compression  $Q = 0$   $\uparrow P \uparrow T \downarrow V$   $\Delta E_{int} = -W$   
( $\uparrow E_{int} \downarrow W$ )

## Carnot Engine

- Example of an ideal heat engine
- Cycle consists of

- 1) isothermal expansion
- 2) adiabatic expansion
- 3) isothermal compression
- 4) adiabatic compression

P vs V Carnot Engine



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Work done by Carnot engine

$$W_{ab} = Q_H$$

$$W_{cd} = -Q_L$$

$$W_{bc} = n C_V \Delta T = n C_V (T_2 - T_H)$$

$$W_{da} = n C_V \Delta T = n C_V (T_H - T_2)$$

$$W_{Net} = W_{ab} + W_{bc} + W_{cd} + W_{da}$$

$$= Q_H + (n C_V T_2 + \cancel{-n C_V T_H}) + -Q_L + (n C_V T_H + \cancel{-n C_V T_2})$$

$$W = Q_H - Q_L$$

$$\Delta S_{gas} = \Delta S_H + \Delta S_L = \Delta S_{cycle} = 0$$

$$\begin{array}{ccc} & \swarrow & \searrow \\ \frac{Q_H}{T_H} & & \frac{Q_L}{T_L} \end{array}$$

\* Temperature of reservoirs remain constant

Relative to the gas  $Q_H$  is positive and  $Q_L$  is negative

$$\frac{Q_H}{T_H} - \frac{Q_L}{T_L} = 0$$

### Efficiency ( $\epsilon$ )

$$\epsilon = \frac{\text{output}}{\text{input}} = \frac{W}{Q_H}$$

work is the desired output.

Energy input is from high temp. reservoir

# Carnot Efficiency

$$\epsilon_c = \frac{W}{Q_H} = \frac{Q_H - Q_L}{Q_H} = 1 - \frac{Q_L}{Q_H} = 1 - \frac{T_L}{T_H}$$

$$\frac{Q_L}{T_L} = \frac{Q_H}{T_H} \Rightarrow \frac{Q_L}{Q_H} = \frac{T_L}{T_H}$$

\* This ( $\epsilon_c$ ) represents the maximum efficiency of a heat engine.

$\Rightarrow$  Implies that all heat engines will operate with an efficiency less than one.

# Refrigerator

- Device used to transfer heat from a low temp. reservoir to a high temp. reservoir.

## Coefficient of Performance (K)

$$K = \frac{\text{output}}{\text{input}} = \frac{Q_L}{W}$$

desired output is removal of heat

work is now an input  
(something must run refrigerator engine)

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## Carnot Refrigerator

$$W = Q_H - Q_L$$

$$\frac{Q_H}{T_H} = \frac{Q_L}{T_L} \Rightarrow \frac{T_L}{T_H} = \frac{Q_L}{Q_H}$$

$$K_C = \frac{Q_L}{Q_H - Q_L} = \frac{Q_L}{Q_H} - 1 = \frac{T_L}{T_H} - 1$$

$$\Delta S = \frac{Q}{T_H} + \frac{-Q}{T_L}$$

$Q$  is amount of heat removed from low temp reservoir

$\Delta S$  is always negative

because  $T_H > T_L$