

# Energy Storage Mechanisms

## Kinetic Energy ( $E_k$ )

$$E_k = \frac{1}{2} m v^2$$

$m = \text{mass (kg)}$

$v = \text{speed (m/s)}$

- Energy stored in a moving object
- object is included in system

## Dissipated Energy ( $E_{\text{diss}}$ )

- Work done by the friction force
- surface is included in the system
- later we will call this internal energy in the thermodynamics chapters

- Energy stored as

random molecular motion

- This energy can only increase

## Gravitational Energy ( $E_g$ )

$$E_g = mgh$$

$m = \text{mass (kg)}$

$g = 9.8 \frac{\text{N}}{\text{kg}}$

$h = \text{height (m)}$

- Energy stored as position in a gravitational field

- Earth or gravitation source is included in system

## Elastic Energy ( $E_{el}$ )

$$E_{el} = \frac{1}{2} k x^2$$

$k$  = spring constant ( $\frac{N}{m}$ )

$x$  = distance from equilibrium (m)

- Energy stored in an ideal spring.
- Spring is included in system.

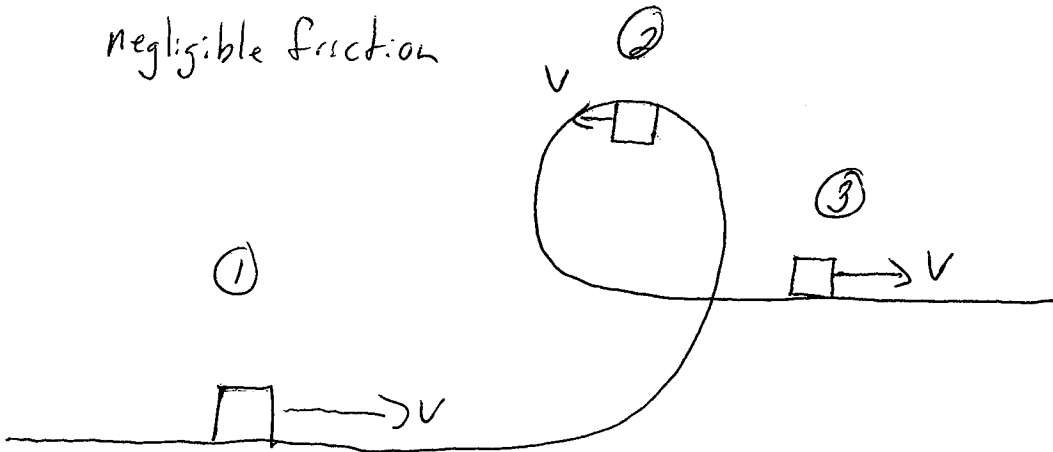
Other energy storage mechanisms exist, but this is all we need for mechanical motion.

## Energy Diagrams

- Pie chart that shows how energy is stored in a system.
- The system is an object or collection of objects that are of interest.
  - \* Choice of a system will involve how we would like to store energy.

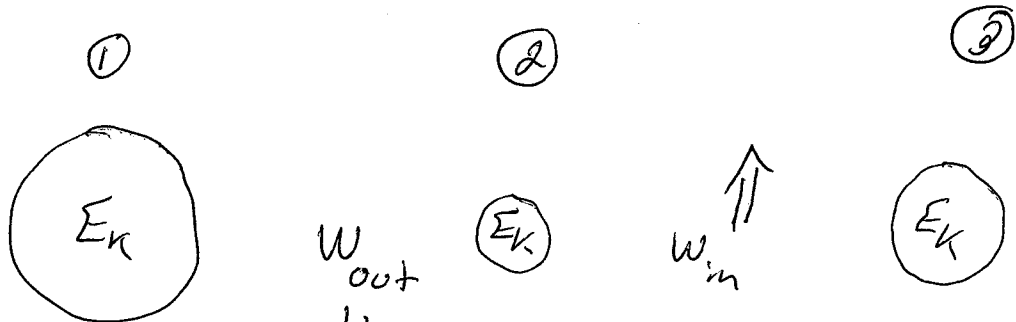
# Energy Diagram Example

negligible friction



Each snapshot in time is (1, 2, 3) characterized by a unique energy diagram.

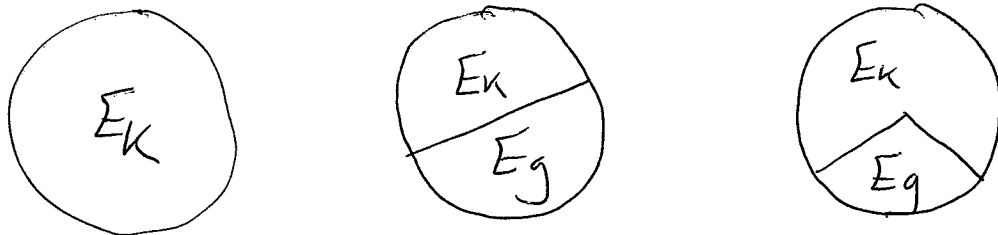
System  
box



$F_g$  does work transferring energy out of box

$F_g$  does work transferring energy into box

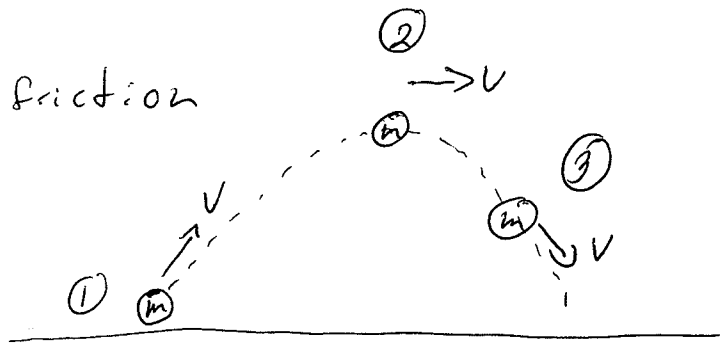
box  
Earth



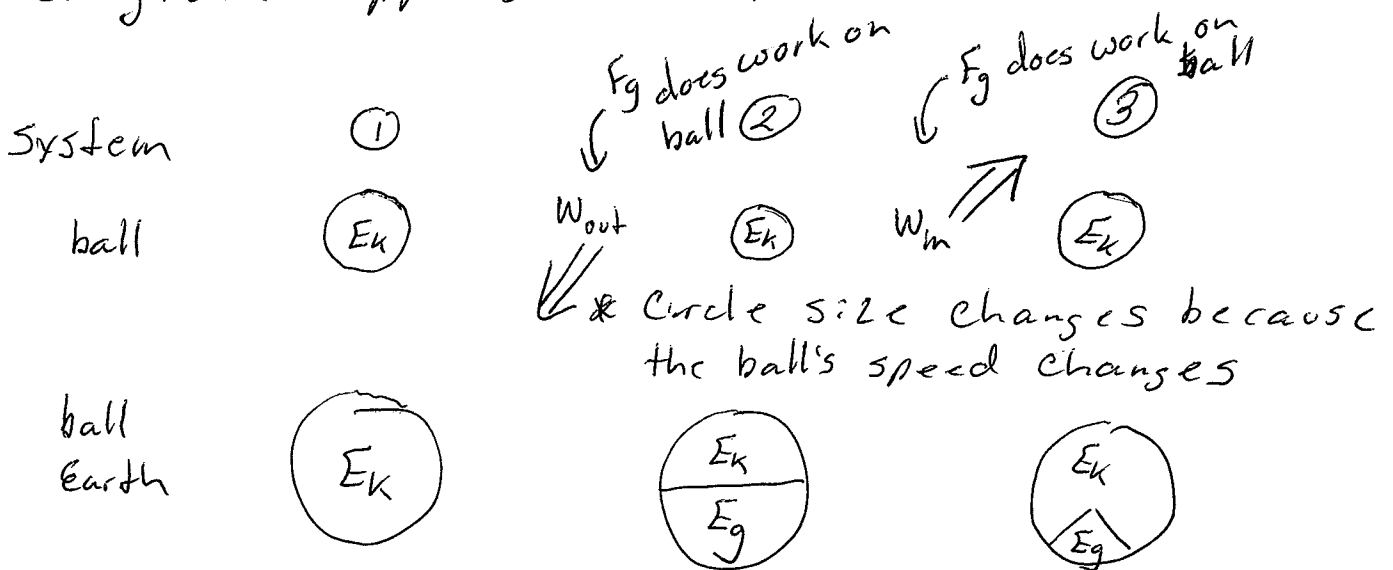
System is large enough so that all energy transfers are internal to the system.

# Energy Diagram Examples

negligible/no friction  
with air



Each snapshot in time (1, 2, 3) shows the system in a different state. An energy diagram applies to only one state.



\* Circle size is constant because the system is large enough to account for all energy transfers that occur during the motion

# Conservation of Energy

- Concept that is useful for analyzing the energy states of a system.
- If the "correct" system is chosen all energy transfers are internal to the system.

In such a case we say that system energy is constant or conserved.

\* When circle sizes are the same we can equate energy equations associated with the diagrams

$E_b$





$$E_g = E_k$$

$$mgh = \frac{1}{2}mv^2$$

$$\Sigma E_g$$

$$\frac{E_k}{E_{diss}}$$

$$\Sigma E_g = E_k + \Sigma E_{diss}$$

$$mgh = \frac{1}{2}mv^2 + W_{\text{friction}}$$

This is why it is most useful to choose a system where all energy transfers are internal.

Another way to state energy conservation

$$\Delta E_{\text{total}} = 0$$

$$\Delta E_{\text{total}} = \Delta E_k + \Delta E_g + \Delta E_{el} + \Delta E_{diss} = 0$$