



$$H = 1.80 \text{ cm}$$

x-axis scale 10.0 cm

$$\Delta t = 6.0 \text{ ms}$$

↓
between A and A'

Two waves with the same amplitude and wavelength travel through a string producing the wave pattern shown above. The equation for wave 1

is: $y(x, t) = y_m \sin(kx + \omega t)$. Determine the equation for the second wave.

Solution: A standing wave pattern is set up by the interference of the two waves.

$$y(x, t) = \underset{\substack{\text{standing} \\ \text{wave}}}{[2 y_m \sin kx]} \cos \omega t$$

(2)

From Graph

$$\lambda = 40 \text{ cm} \quad \frac{1}{2}H = y(10 \text{ cm}, t) = \underbrace{[2y_m \sin kx]}_{\text{Amplitude}} \cos \omega t = 0.90 \text{ cm}$$

Given

$$\frac{1}{2} T = 6.0 \text{ ms}$$

$$T = 12.0 \text{ ms} = 12.0 \times 10^{-3} \text{ s}$$



$$k = \frac{2\pi}{\lambda} = \frac{2\pi}{40 \text{ cm}} = 0.1571 \text{ cm}^{-1}$$

$$0.90 \text{ cm} = 2y_m \sin(0.1571 \text{ cm}^{-1} \cdot 10 \text{ cm})$$

$$\omega = \frac{2\pi}{T} = 524 \text{ s}^{-1}$$

$$\frac{0.90 \text{ cm}}{2 \sin[0.1571(10)]} = y_m$$

$$0.45 \text{ cm} = y_m$$

$$y(x, t) = y_m \sin(kx - \omega t) \quad \downarrow \text{opposite the 1st wave}$$

$$y(x, t) = 0.45 \text{ cm} \sin(0.1571 \text{ cm}^{-1} x - 524 \text{ s}^{-1} t)$$